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A particle swarm optimization for the vehicle routing problem with simultaneous pickup and delivery

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ABSTRACT

This paper proposes a formulation of the vehicle routing problem with simultaneous pickup and delivery (VRPSPD) and a particle swarm optimization (PSO) algorithm for solving it. The formulation is a generalization of three existing VRPSPD formulations. The main PSO algorithm is developed based on GLNPSO, a PSO algorithm with multiple social structures. A random key-based solution representation and decoding method is proposed for implementing PSO for VRPSPD. The solution representation for VRPSPD with n customers and m vehicles is a (n+2m)-dimensional particle. The decoding method starts by transforming the particle to a priority list of customers to enter the route and a priority matrix of vehicles to serve each customer. The vehicle routes are constructed based on the customer priority list and vehicle priority matrix. The proposed algorithm is tested using three benchmark data sets available from the literature. The computational result shows that the proposed method is competitive with other published results for solving VRPSPD. Some new best known solutions of the benchmark problem are also found by the proposed method.

Scope and Purpose

This paper applies a real-value version of particle swarm optimization (PSO) algorithm for solving the vehicle routing problem with simultaneous pickup and delivery (VRPSPD). The VRPSPD formulation is reformulated and generalized from three existing formulations in the literature. The purposes of this paper are to explain the mechanism of the PSO for solving VRPSPD and to demonstrate the effectiveness of the proposed method.

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1. Introduction

The vehicle routing problem (VRP) is a generic name given to a class of problems to determine a set of vehicle routes, in which each vehicle departs from a given depot, serves a given set of customers, and returns back to the same 38 ot. Various types of service appear in practical situations, while physical delivery of goods is the most common one.

The basic VRP involves a single depot, a fleet of identical vehicles that stations at the depot, and a set of customers who require delivery of goods from the (15)t. The objective of basic VRP is to minimize the total routing cost, subject to maximum working time and maximum capacity constraints on the vehicles [1]. Besides the basic VRP, many VRP variants may appear since there are many possibilities in

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0305-0548/\$ - see front matter © 2008 Elsevier Ltd. All rights reserved. doi:10.1016/j.cor.2008.04.003 real-life problem settings and characteristics, for example: the number of depots, ty 22 f vehicle, and customer requirements. Toth and Vigo [2] provide comprehensive details on VRP, its variants, formulating and solution methods.

One extension of the basic VRP is the vehicle routing problem 15 h simultaneous pickup and delivery (VRPSPD). In this variant, customers require not only the delivery of goods but also the simultaneous pick up of goods from them. A general assumption is that all delivered good 10 ignate from the depot and all pickup goods must be transported back to the depot. Min [3] was inspired by a distribution problem of a public library and first introduced this extension as the VRPSPD for minimizing the total travel time of the route by considering the vehicle capacity as the problem constraint. His proposed solution procedure for the problem consists of three phases: clustering customer nodes, assigning vehicles to clusters, and creating 34 route of each vehicle.

After Min [3], some researchers also contributed on the mathematics formulation of VRPSPD and the solution techniques. Dethloff [4] discussed the importance of VRPSPD in the reverse logistic

operations. He proposed a mathematical formulation for the problem to minimize the total traveled distance, subject to maximum capacity constraint of the vehicle. He also developed an insertion-based heuristic that use four different criteria to solve the problem.

Salhi and Nagy [5] proposed four insertion-based heuristics for generating solution for VRPSPD. The basic steps of these heuristics are constructing partial routes for a set of customers 50 d then inserting the remaining customers to the existing route. These heuristic rules were differentiated mainly 15 the criteria for insertion and number of customers per insertion. Nagy and Salhi [6] also proposed a logical search heuristic with four phases to solve VRPSPD. After finding an initial solution in the first phase, it is continuously improved in each of the following phases while maintaining a certain feasibility condition. In both papers, they addressed not only the VRPSPD, but also the mixed case of VR 15 here some customers require delivery and the other customers require pickup. They showed that the VRPSPD is a generalization of the mixed problem. In addition, they als 7 xtended the method for the multi depot case.

Tang and Galvao [7] developed a tabu search algorithm to solve VRPSPD. The algorithm combines several efforts to obtain alternative inter-route and intra-route solutions, includes relocation of a customer from one route to another route, interchange a pair of customers 10 ween two routes, crossover two routes, and 2-opt procedure. In their formulation, the VRPSPD is formulated to minimize the total traveled distance of the route subject to maximum distance and maximum capacity constraints on the vehicles.

Bianchessi and Righini [8] proposed heuristic algorithms for solving VRPSPD. Their work comprised of four different constructive algorithms, local search algorithms with various neighborhood structures, and tabu search algorithms. They were using Dethloff's VRPSPD formulation and their computational result outperformed resuzy in Dethloff [4].

Dell'Amico et al. [9] was the first published work on exact method for solving VRPSPD. They presented an optimization algorithm based on column generation, dynamic programming, and branch and price method. However, the computational complexity of VRPSPD is evident from the computational result, in which 1 h of computational time sometimes is not enough for solving a small size problem consist of 498 ustomers.

It is noted that the VRPSPD can be seen as a pickur 411d delivery problem (PDP). In the recent classification 23 static pickup and delivery problem by Berbeglia et al. [10], the VRPSPD is called the multi-vehicle Hamiltonian one-to-many-to-one pickup and 23 ivery problem with combined demands. By this definition, the problem consists of multi vehicles which its routes are a Hamiltonian cycle; the deliveries are from depot and the p 23 ps will be transferred back to depot (one-to-many-to-one); the customer demand is combined which means that at least there is one customer with non zero pic p and delivery demand.

PSO is a population-based search method proposed by Kennedy and Eberhart [11], which motivated by the group organism behavior such as bee swarm, fish school, and bird flock. PSO imitated the physical movements of the individuals in the swarm as a searching method. A brief and complete survey on PSO mechanism, technique, and application is provided by Kennedy and Eberhart [12] and also Clerc [13]. While some other population-based search methods had been successfully applied in broader area of VRP, such as genetic algo 68 m [14-16] and ant colony optimization [5,18], the application of PSO on VRP is still rare. One is the work of Chen et al. [19], where the discrete version of PSO is combined with Simulated Annealing (SA) algorithm for solving the basic VRP.

Tl 57 are two main contributions of this paper. First, it reformulates the VRPSPD as a direct extension of the basic VRP. As a result, the formulation of Min [3], Dethloff [4], Tang and Galvao [7] can be reduced to a special case of this reformulation. Second, it fills the

gap of the a 16 cation of PSO for VRP solution by showing how the real-valued version of PSO is applicable for solving VRPSPD.

The proposed algorithm in this paper is different from Chen's algorithm [19] in two aspects. First, the algorithm uses real value instead of discrete value for search variables. Second, it is implemented withou he use of any local search method.

The remainder of this paper is organized as follows: Section 2 reviews the VRPSPD definition and mathematical formulation. Section 3 describes the proposed PSO algorithm for solving VRPSPD. Section 4 discusses the computational experiment of the proposed PSO on a benchmark data set. Finally, Section 5 concludes the result of this research and suggests further direction of the future research.

2. VRPSPD formulation

The VRPSPD can be formally defined as follows. Let G = (V, A) be a graph where $V = \{v_0, v_1, \dots, v_n\}$ is a vertex 35, and $A = \{(v_i, v_j) | v_i, v_j \in$ $V,i \neq j$] is an arc set. Associated with i3 re a distance matrix (d_{ij}) and a travel time matrix (t_{ij}) . Vertex v_0 represents a depot at which m homogeneous vehicles are stationed, while the remaining vertices correspond to n customers. Each customer has a non-ne 20 ve pickup quantity p_i , delivery quantity q_i , and a service time s_i . Every vehicle has a fixed cost of f, variable $\frac{1}{26}$ per distance unit g, capacity Q, and service duration limit D. The VRPSPD consists of designing a set of at most m routes such that

- (1) each route starts and ends at the depot;
- (2) each customer is visited exactly once by exactly one vehicle;
- (3) the total vehicle load in any arc does not exceed the capacity of the 5 hicle assigned to it (Q);
- (3) the total duration of each route (including travel and service times) does not exceed a preset limit D; and
- (4) the total routing cost is minimized.

The mathematical formulation of VRPSPD is presented below following the pregiding definition, which is a network flow-based formulation and a mixed integer linear program (MILP). The formulation is an extension of Christofides' basic VRP formulation [1].

Decision variables:

a binary variable indicating whether arc (i, j) is traversed by vehicle k

 $x_{ijk} = 1$ if vehicle k traverses arc (i, j)

= 0 if vehicle k does not traverse arc (i, j)

 $\frac{1}{34}$ d of vehicle k while traverses at $\frac{1}{67}$ j)

 δ_{ik} starting second Objective function starting service time of customer i by vehicle k

Minimize
$$Z = f \sum_{k=1}^{m} \sum_{j=1}^{n} x_{0jk} + g \sum_{i=0}^{n} \sum_{j=1}^{n+1} \sum_{k=1}^{m} d_{ij} x_{ijk}$$

3 Subject to
$$\sum_{i=0}^{n} \sum_{k=1}^{m} x_{ijk} = 1 \quad \text{for } 1 \le j \le n$$
(2)

$$\sum_{j=0}^{n} x_{jik} = \sum_{j=1}^{n+1} x_{ijk} \quad \text{for } 1 \leqslant i \leqslant n, \ 1 \leqslant k \leqslant m$$
 (3)

$$\sum_{j=0}^{n} x_{0jk} \leqslant 1 \quad \text{for } 1 \leqslant k \leqslant m \tag{4}$$

$$\delta_{ik} + s_i + t_{ii} - \delta_{ik} \leqslant (1 - x_{iik})M$$
 for $0 \leqslant i \leqslant n$, $1 \leqslant j \leqslant n + 1$, $1 \leqslant k \leqslant m$ (5)

$$\delta_{n+1,k} - \delta_{0k} \leqslant D \quad \text{for } 1 \leqslant k \leqslant m \tag{6}$$

(9)

(10)

$$y_{ijk} \leqslant x_{ijk}Q$$
 for $0 \leqslant i \leqslant n$, $1 \leqslant j \leqslant n+1$, $1 \leqslant k \leqslant m$

$$\sum_{i=1}^{n} y_{0jk} = \sum_{i=1}^{n} q_j \sum_{i=0}^{n} x_{ijk} \quad \text{for } 1 \le k \le m$$
 (8)

$$\sum_{i=0}^{n} y_{ijk} + (p_j - q_j) \sum_{i=0}^{n} \frac{75}{x_{ijk}} = \sum_{i=1}^{n+1} y_{jik}$$

$$x_{iik} \in \{0, 1\}$$
 for $0 \le i \le n$, $1 \le j \le n + 1$, $1 \le k \le m$

$$y_{ijk} \geqslant 0 \quad \text{for } 0 \leqslant i \leqslant n, \quad 1 \leqslant j \leqslant n+1, \quad 1 \leqslant k \leqslant m$$
 (11)

$$\delta_{ik} \geqslant 0 \quad \text{for } 0 \leqslant i \leqslant n+1, \quad 1 \leqslant k \leqslant m$$
 (12)

The objective function (1) shows that this model minimizes routing cost, which consists of transportation fixed cost and variable cost, Constraints (2) and (3) form the feasible routes of vehicles, so that every customer is visited by exactly one vehicle (2), every vehicle that arrives to a customer must leave that customer (3), and vehicle is used to serve at most one route.

Constraints (5) and (6) explain the relationship 3 ween time variables and parameters in this model. Constraint (5) regres the starting service time of one customer with other customer. If vehicle k serving 34 stomer j after serving customer i ($x_{ijk}=1$), starting service time in customer j must be greater or equal to the sum of starting 65 rice time in customer i, the service time and transportation time from customer i to customer j ($\delta_{ik}+s_i+t_{ij}\leqslant \delta_{jk}$). Otherwise, there is not trict relationship between those starting service time (δ_{ik} and δ_{jk}) when $x_{ijk}=0$. Furthermore, δ_{0k} represents the time when vehicle k depart from the depot (it is assumed that a vehicle is 164 y to go at the beginning of a planning horizon, $s_0=0$) and $\delta_{n+1,k}$ represents the time when vehicle k return to the depot. Hence, the difference between the latter and the former represents the service/working duration of vehicle k and the limit of service duration is stated in corganit (6).

Vehicle load constraints are explained in (7)–(9). Constraint (7) states that if vehicle k serving customer j after serving customer i ($x_{ijk} = 1$), the corresponding load (y_{ijk}) must at most equal to the vehicle load capacity (Q); and otherwise the load $y_{ijk} = 0$ if $x_{ijk} = 0$. Constraint (8) assures that all customer deliveries are from the depot. It states that the load of a vehicle at the departure from the depot must be equal to the total load for customer deliveries of the corresponding vehicle. Constraint (9) balances the load of a vehicle after it serves a customer 30

Constraints (10)–(12) state the domain of decision variables: all x_{ijk} are binary variables, y_{ijk} and δ_{ik} are non-negative real variables. Especially for δ_{ik} , it has the meaning of starting service time of customer i by vehicle k only when customer i are served by vehicle k ($x_{ijk}=1$ and consequently $x_{jik}=1$).

This formulation can be seen as a general model of VRPSPD. By setting the parameters, this model could lead to previously proposed model of VRPSPD. The formulation reduces to Min's [3] by setting the fixed cost f=0, the variable cost g=1, $d_{ij}=t_{ij}$ in Eq. (1), and the service durat [1] limit of vehicle $D=\infty$. The formulation reduces to Dethloff's [4] by setting the fixed cost f=0, variable cost g=1, and servite duration limit $D=\infty$. To reduce to Tang and Galvao's [7], set the fixed cost f=0, the variable cost g=1, the service time $s_i=0$, define $t_{ij}=d_{ij}$, and define D=0 as the maximum distance allowed per vehicle.

3. PSO for VRPSPD

In this section, a particle swarm optimization (PSO) algorithm is proposed for solving the general formulation of VRPSPD that is

described in Section 2. Key features of the algorithm are explained in details including solution representation, decoding procedure to map representation to problem solution, and additional routine for searching appropriate number of vehicles.

3.1. PSO algorithm

As mentioned before, PSO is a population-based search method that imitated the physical movements of the individuals in the swarm as a searching method. In the PSO, a swarm of L particles is served as searching agent for a specific problem solution. A particle's position (Θ_l), which consists of H dimensions, is representing a solution of the problem. The ability of a particle to search for solution is represented by its velocity vector (Ω_l) which drives particle movement. In the PSO iteration step, every particle moves from one position to another position based on its velocity. Moving from one position to another, a particle is evaluating different prospective solenois of the problem.

PSO also imitated swarm's cognitive and social behavior as local and global search abilities. In the basic version of PSO, the particle's personal best position (Ψ_l) and the global best position (Ψ_g) are always updated and kept. The personal best position of a particle, which expresses the cognitive behavior, is defined as the position that gives the best objective function among the positions that have been visited by the particle. Once a particle reaches a position that has a better objective function than the previous best objective function for this particle (i.e. $Z(\Theta_l) < Z(\Psi_l)$), the personal best position is updated. The global best position, which expresses the social behavior, is the position that gives the best objective function among the positions that have been visited by all particles in the swarm. Once a particle reaches a position that has a better objective function than the previous best objective function for whole swarm (i.e. $Z(\Psi_l) < Z(\Psi_g)$), the global best position is also updated.

The personal best and global best positions are used for updating particle velocity. In each iteration step, the velocity Ω is updated based on three terms: inertia, cognitive learning and social learning terms. The inertia term forces a particle to move in the same direction as previous iteration. The 12 rm is calculated as a product of current velocity with an inertia weight (w). The cognitive term forces a particle to go back to its personal best position. This term is calculated as a product of a random number (u), personal best acceleration constant (c_p) , and the difference between personal best position Ψ_l and current position Θ_l . The social term forces a particle to move to the global best position. This term is calculated as a product of a random number (u), global best acceleration constant (c_g) , and the difference betwee Θ_l lobal best position Ψ_g and current position Θ_l .

In the velocity-updating formula, random numbers are incorporated in order to randomize particle movement. Hence, two different particles may move to different position in the subsequent iteration even though they have similar position, personal best, and global best. Inertia weight and acceleration constants are the parameters that affect particle movement, each of them give the religive weight to the inertia, cognitive, and social term, respectively. High inertia weight means the particles tends to maintain current direction and low inertia weight mear the particles tends to follow the cognitive and social term. It is common to have high inertia weight at the beginning of PSO iteration and low weight at the end, so that the particles are mov 44 more freely to explore the solution space in the initial phase and following the cognitive and social tean to exploit the personal best and global best in the final phase. It is expected that the particles can find a high quality personal and global best during the exploration phase, then the personal and global best can be used as good movement guidance in the exploitation phase.

In the PSO particle movement mechanism, it is also common to limit the search space of particle location, i.e. the position value of particle dimension is bounded at value $[\theta^{\min}, \theta^{\max}]$. This feature

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exists as the mechanism to avoid solution divergence. Hence, the position value of certain particle dimension is being set at the minimum or maximum value whenever it moves beyond the boundary. In addition, the velocity of corresponding dimension is reset to zero to avoid further movement b 74 nd the boundary.

PSO works on finding 5 be best position and the position is represented by a real number. To make PSO applicable to specific problem; the relationship between the position of particles and the solutions of that problem must be clearly defined. In VRP case, the particle's position represents the vehicle route. The details of the proposed solution representation and its relationship with vehicle route are described in the Sec 8 ns 3.2 and 3.3.

A PSO algorithm for solving VRPSPD is proposed here based on the GLNPSO, a PSO Algorithm 31th multiple social learning structures [20]. In this PSO version, the component for social learning behavior includes not only the global best but also the local best (Ψ_I^L) and near neighbor best (Ψ_I^N) . The local best is the best position of among several adjacent particles. The near neighbor best is a 56 al learning behavior concept proposed by Veeramachaneni [21]. It is determined based on fit 12 s-distance-ratio (FDR). The formula for determining these terms in the velocity updat 29 formula is similar with the social arm in the basic PSO, which is a product of a random number (u), an acceleration constant (c_l or c_n), and the difference between the

social component $25 \frac{V}{I}$ or $\frac{V_I^N}{I}$ and current position Θ_I .

The details of the PS 13 gorithm for solving VRPSPD are presented below in Algorithm 1. In this algorithm, the particles are initialized in step 1, their corresponding fitness value are evaluated in steps 2-3, their cognitive and social infor 5 tion are updated in steps 4-7, and their positions are updated in step 8. Step 9 is the controlling step to repeat or stop the iteration. Note that the problem-specific steps are the conversion of particle's position into vehicle route in step 2, and, the determination of the performance measurement of

the 13 Ite in step 3. Notation

 Ψ_l

 Ψ_{i}^{L}

 $[\psi_{l1} \ \psi_{l2} \ \cdots \ \psi_{lH}]$

 $[\psi_{I1}^L \ \psi_{I2}^L \ \cdots \ \psi_{ID}^L]$

the Ith set of vehicle route

```
iteration index; \tau = 1 \dots T
       particle index, l = 1 ... L
       dimension index, h = 1...H
h
       uniform random number in the interval [0, 1]
w(\tau) inertia weight in the \tauth iteration
\omega_{lh}(\tau) velocity of the lth particle at the hth dimension in
       the τth iteration
\theta_{lh}(\tau) position of the lth particle at the hth dimension in
       the τth iteration
       personal best position (pbest) of the Ith particle at
\psi_{lh}
       the hth dimension
       global best position (gbest) at the hth dimension
       local best position (lbest) of the lth particle at the
\psi_{lh}^{L}
       hth dimension
       near neighbor best position (nbest) of the Ith particle
       at the hth dimension
       personal best position acceleration constant
c_p
       global best position acceleration constant
c_g
       local best position acceleration constant
c_I
       near neighbor best 12 tion acceleration constant
       maximum position value
\theta^{\min}
       minimum position value
```

vector position of the *l*th particle, $[\theta_{l1} \ \theta_{l2} \ \cdots \ \theta_{lH}]$

vector velocity of the *l*th particle, $[\omega_{l1} \ \omega_{l2} \ \cdots \ \omega_{lH}]$

vector personal best position of the Ith particle,

vector local best position of the 1th particle,

vector global best position, $[\psi_{g1} \ \psi_{g2} \ \cdots \ \psi_{gH}]$

```
(\Theta_l) fitness value of \Theta_l
FDR fitness-distance-ratio
```

Algorithm 1 (PSO Algorithm for VRPSPD).

- 1. Initialize L particles as a swarm, generate the l_{14} article with random position Θ_l in the range $[\theta^{\min}, \theta^{\max}]$, velocity $\Omega_l = 0$ and personal best $\Psi_l = \Theta_l$ for $l = 1 \dots L$. Set iteration $\tau = 1$.

 4 for $l = 1 \dots L$, decode $\Theta_l(\tau)$ to a set of vehicle route R_l .
- 3. For $l = 1 \dots L$, compute the performance measurement of R_l , and set this as the fitness value of Θ_l , represented by $Z(\Theta_l)$.
- 4. Update pbest: For $l=1\ldots L$, update $\Psi_l=\Theta_l$, if $Z(\Theta_l)< Z(\Psi_l)$. 5. Update gbest: For $l=1\ldots L$, update $\Psi_g=\Psi_l$, if $Z(\Psi_l)< Z(\Psi_g)$.
- 6. Update lbest: For $l = 1 \dots L$, among all pbest from K neighbors of the Ith particle, set the personal best which obtains the least fitness value to be Ψ_I^L .
- 7. Generate nbest: For l=1...L, and h=1...H, set $\psi_{lh}^N=\psi_{oh}$ that maximizing fitness-distance-ratio (FDR) for o = 1...H. Where FDR is defined as

$$FDR = \frac{Z(\Theta_l) - Z(\Psi_0)}{|\theta_{lh} - \psi_{oh}|} \quad \text{where} \quad l \neq 0$$
 (13)

8. Update the velocity and the position of each Ith particle:

$$w(\tau) = w(T) + \frac{\overline{\tau} - T}{1 - T} [w(1) - w(T)]$$
(14)

$$\omega_{lh}(\tau+1) = w(\tau)\omega_{lh}(\tau) + c_p u(\psi_{lh} - \theta_{lh}(\tau)) + c_g u(\psi_{gh} - \theta_{lh}(\tau))$$

$$+c_l u(\psi_{lh}^L - \theta_{lh}(\tau)) + c_n u(\psi_{lh}^N - \theta_{lh}(\tau)) \tag{15}$$

$$\theta_{lh}(\tau+1) = \theta_{lh}(\tau) + \omega_{lh}(\tau+1) \tag{16}$$

If
$$\theta_{lh}(\tau+1) > \theta^{max}$$
, then

$$\theta_{lh}(\tau + 1) = \theta^{\text{max}} \tag{17}$$

$$\omega_{lh}(\tau+1) = 0 \tag{18}$$

If
$$\theta_{lh}(\tau+1) < \theta^{\min}$$
, then

$$\theta_{lh}(\tau+1) = \theta^{\min} \tag{19}$$

$$\omega_{\rm IL}(\tau+1) = 0 \tag{20}$$

9. If the stopping criterion is met, i.e. $\tau = T$, stop. Otherwise, $\tau = \tau + 1$ and return to step 2.

3.2. Solution representation

Solution representation of vehicle routes is one of the key elements for effective implementation of PSO for VRPSPD. An indirect representation is proposed here. It consists of two parts: the first part is related to the customers and the second part is related to the vehicles. This representation is decoded into vehicle routes by steps describ

The first part of the representation is required to set priority f customer to enter existing route in the route construction step. A random key with n elements is applied here. The first part of the representation consists of *n* dimensions of particle with each dimension assigned to a customer. The spaller value of the dimension corresponds to the higher priority to the customer.

The second part of the representation is based on the idea of vehicle route orientation. Route 52 ntation of a vehicle is defined as a point in the service map that represents a certa 8 area in which the vehicle is most likely to serve. Consequently, a vehicle route will tend to aggregate around its corresponding route orientation. A simple illustration of relationship between vehicle route and route



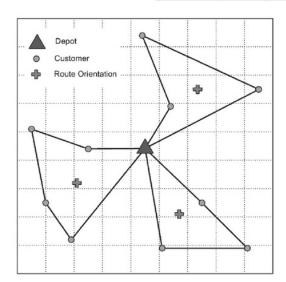


Fig. 1. Vehicle routes and route orientation.

orientation is depicted in Fig. 1. It is clearly seen that each vehicle covers certain service area that can be represented by the route origination point.

A route orientation point is identified by its x–y coordinate in the service map. Since PSO uses position of particle with many dimensions to represent solution and the position values are a real numbers, each rout a rientation can be represented by two dimensions of a particle, one dimension for x-coordinate value and the other dimension for y-coordinate value. Hence, the second part of the representation would consist of 2m dimensions of particle that correspond to m available vehicles.

The route orientation is used as another basis for route construction. After all the route orientations are identified, preference of vehicles to serve each customer could be determined based on the distance of customer to orientation point. These preferences are set to ensure the spatial closeness among customers in one route, since the spatial closeness between customer and route orientation are initiatined. While the spatial closeness is sustained, the total route distance might be shorter and the corresponding variable cost could be minimized.

are determined based on the coverage of the service map. This boundary is very crucial for the particle's dimensions related to the vehicles, where the vehicle route orientation represented by these dimensions cate placed at every location in the service map. Hence, the minimum value of x-axis and y-axis of the service map is set as the minimum boundary θ^{\min} and the maximum value of x-axis and y-axis of the service map is set as the maximum boundary θ^{\max} . This boundary has no effect for the particle's dimensions related to the customers; however, the same boundary values are also selected for these dimensions.

In summary, the proposed solution representation of VRPSPD with n customers and m vehicles will require particle with (n+2m) ension. Each particle dimension is encoded as a real number. The first n dimensions represent priorities of customers, each customer is represented by one dimension. The values in these dimensions are converted to customer priority list in the decoding step. The other 2m dimensions are related to vehicles, each vehicle is represented by two dimensions. These dimensions are extracted as the orienta-

tion point of vehicles in the Cartesian diagram/map. The summary of solution representation and its main conversion are displayed in Fig. 2.



Three steps must be taken in order to decode the proposed solution representation described in previous sect 5 into the VRPSPD solution. First, extract the information from the lirst *n* dimension to make a priority list of customers. Second, take the information from the last 2*m* dimension to determine the route orientation point of vehicles and use this info 22 ation to create priority matrix of vehicles. Third, construct the vehicle routes based on the customer priority list and vehicle priority less tix.

ority list and vehicle priority
In the first step, after the first n dimension of position value is removed, the customer priority list is constructed following the rule mentioned 21 previous sub-section. The simplest implementation of this rule is by sorting in ascending order the position value and taking the dimension index as the list.

The next step is to extract the route orientation point of vehicles an 5 construct priority matrix of vehicle. The matrix is constructed based on the relative distance between these points and customers location. The distances can be calculated in every case of VRPSPD, since the location of customers is placed in a two-dimensional/Cartesian map. A customer is served first by vehicle with closer distance. Each row in the matrix keeps the vehicle priority for customers with the same priority.

The last decoding step is to construct a route based on the customer priority list and the vehicle priority matrix. One by one, each customer in the customer priority list is assigned to a vehicle based on its priority and such problem constraints as vehicle capacity constraint and service duration constraint. This newly assigned customer is inserted to the best position in the existing vehicle route based on the least diditional cost. This is called the cheapest insertion heuristic. Another effort to improve solution quality of the route is to re-optimize the emerging route us 25 some improvement heuristic methods such as 2-opt method. The details of this decoding procedure are described in Algorithm 2.

Algorithm 2 (Decoding method)

Decoding particle position (θ_{lh} -position of the lth particle at the hth dimension) in vehicle route (R_{lj} -route of the jth vehicle corresponding to the lth particle)

- 1. Construct the priority list of customers (U)
 - a. Build set $S = \{1, 2, ..., n\}$ and $U = \emptyset$
- b. Select c from set S where $\theta_{lc} = \min_{h \in S} \theta_{lh}$
- c. 76 c to the last position in set U
- d. Remove c from set S
- e. Repeat step 1.b until $S = \emptyset$
- 2. Construct the vehicle priority matrix (W)

a. Set the vehicle reference position. For $j = 1 \dots m$,

set $xref_j = \theta_{l,n+2j-1}$ and $yref_j = \theta_{l,n+2j}$

b. For each customer $i, i = 1 \dots n$

i. Calculate the Euclidean distance between customer *i* and vehicle route orientation points using following formula

$$\Delta_j = \sqrt{(xpos_i - \frac{73}{xref_j})^2 + (ypos_i - \frac{yref_j}{2})^2}$$
 (21)

ii.Build set $S = \{1, 2, ..., m\}$ and $W_i = \emptyset$ iii. Select c from set S where $\Delta_c = \min_{i \in S} \Delta_i$

iv. Add c to the last position in set W_i

v. Remove c from set S

vi. Repeat step 2.b.iii until $S = \emptyset$

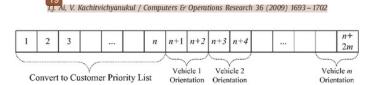


Fig. 2. Solution representation and its conversion.

3. Construct vehicle route

a. Set k=1

b. Add customer one by one to the route

i. Set $c = U_k$ and b = 1

ii. Set $j = W_{c,b}$

iii. Make a candidate of new route by inserting customer 5 of the best sequence in the route R_{ij} (route of vehiclej), which has the smallest additional cost (the cheapest in 3 ion heuristic)

iv. Check feasibility of the candidate route by evaluating all constraints: vehicle capacity and service duration constraints

v. If a feasible solution is reached, update the route R_{ij} with the candidate route and re-optimize emerging sute with 2-opt method; then go to step 3.c

vi. If b=m, go to step 3.c. Otherwise, set b=b+1 and repeat from step 3.b.ii

c. If k = n, stop. Otherwise, set k = k + 1 and repeat step 3.b.

Following this decoding method, there is a possibility that a customer was not inserted into any routes. This situation is undesirable because some customers are not served and this corresponds to an infeasible solution. To avoid particle position that represents kind of solution from being a candidate of best position, a large penalty is added to the fitness value of the particle for each customer not served. By this means and the principles of particle movement in the PSO, a particle that represents infeasible solution tends to move toward a position with lower degree of infeasibility and may eventually lead to a feasible solution.

3.4. Searching for appropriate number of vehicles

The proposed solution representation decoding method is designed for solution of VRPSPD with fixed 48 nber of customers (n) and 63 ed number of vehicles (m). It is true that for most problems, the numb(62) customers to be served is fixed and known in advance. Hov 162 rt, the number of vehicles that actually serve the customers is a decision variable, which may have a value less than the number of availage vehicles.

One advantage of this representation is its tendency to spread evenly the service area of vehicles. In other words, all available vehicles are more likely to be used to serve the customers. Since the variable to extra the tendency to reduce the main contributor of the total cost, it is necessary to reduce the number of vehicles that are active in serving the customers. Hence, an additional routine is proposed here to obtain appropriate number of vehicle. This routine is implemented in the initialization step (Step 1) of PSO algorithm.

The main idea of this routine is to reclice the number of vehicles one by one while initializing a particle. Starting with the number of available vehicles, a solution representation is generated. After it is decoded, the number of customers served by each route is evaluated by trying to remove two particle dimensions corresponded to vehicle with smallest number of customers served. If the new representation leads to better fitness value, repeat the removal proced 47 intil further removal lead to an inferior fitness value. Figure 11, the number of vehicles (m) is set to the number that gives the best fitness value. To speed up the process, this number is immediately used as the

number of available vehicles in the process to generate subsequent particles. The detail of this routine is explained in Algorithm 3.

Algorithm 3 (Routine to search for appropriate number of vehicles).

- 1. Generate a random partic q to represent n customers and m vehicles, which consists of n + 2m dimensions. Set v = m.
- Decog the particle into vehicle routes using Algorithm 2. Compute the performance measurement of the route, and set this value as the fitness value of the particle, Z.
- 3. Calculate the number of customers served by each vehicle.
- 4. Remove the corresponding dimensions of the vehicle with smallest number of customers. Reduce the particle size by two dimensions. Set v = v 1.
- 5. Detade the updated particle into vehicle routes using Algorithm 2. Compute the performance measurement of the route, and set this value as the fitness value of the updated particle, Z'.
- 6. If the fitness value of updated particle is smaller than its of original particle, Z' < Z, set Z = Z', then repeat step 3–5; otherwise, go to step 7.
- 7. Add back the two particle dimensions last removed. Increase the particle size by two dimensions. Set v = v + 1. Then, set the new value of number of available vehicles m = v for subsequent particles.

4. Computational result

4.1. Comparison with results from literature

Computational experiments are conducted by applying this proposed algorithm to some benchmark data sets of VRPSPD in order to evaluate the performance of the profession of th

The algorithm is implemented in C# language using Microsoft Visual Studio.NET 1.1 on a PC with Intel P4 3.4 GHz—1 GB RAM. For each data set, 37 eplications of the algorithm are tried. The PSO parameters are set based on the result of some preliminary experiments that are carried out to observe the behavior of algorithm in different parameter setting. The PSO parameters are summarized in Table 1.

4.1.1. Dell'An 20 data

The first computational experiment is conducted on the benchmark data set of Dell'Amico et al. [9] which comprises five classes

4 ble 1 Summary of PSO parameters.

Parameter	Value
Number of particle	L = 50
Number of iteration	T = 1000
Number of neighbor	K = 5
First inertia weight	w(1) = 0.9
Last inertia weight	w(T) = 0.4
Personal best position acceleration constant	$c_p = 1$
Global best position acceleration constant	$c_g = 0$
Local best position acceleration constant	$c_l = 1$
Near neighbor best position acceleration constant	$c_n = 2$

Table 2
Comparison of Dell'Amico et al. and PSO solution.

Instance class	Average total cost	
20	Dell'Amico et al. [9]	PSO
Class 1	522.5	524.7
Class 2S	236822.7	236826.4
Class 2C	341481.2	341994.3
Class 3S	12082.3	11912.3
Class 3C	15979.6	15984.6

of VRPSPD instances. Each class consists of instances with 20 and 40 customers. Class 1 consists of 12 instances, while Class 2S, 2C, 3S, and 3C consist of 18 instances. The VRPSPD of these instances is similar to the Dethloff formulation. Hence, the following problem parameters are required to be set in the proposed PSO method: fixed cost per vehicle, f=0; variable cost per distance unit, g=1; service duratig limit $D=\infty$; and the number of available vehicles is equal to the number of available vehicle in the optimal/best known solution.

The comparison of the best solution among 10 PSO iterations with the 20 per bound result of Dell'Amico et al. [9] is presented in Table 2, in which the average total cost of the instances in each class is compared. It is noted that Dell'Amico et al. [9] already provided the optimal solution 40 75 out of 84 instances. Hence, the upper bound represents the 33 timal solution or the best solution found. The 20 llt presented in Table 2 implies that the proposed PSO method is able to provide high quality solutions that are very close to the optimal solution. Moreover, these solutions can be obtained in very short computational time, in average of 9 and 27 s, respectively, for 20-customer and 40-customer problems.

4.1.2. Dethloff data

Th 9 econd computational experiment is conducted on the bench18 k data set of Dethloff [4] which comprises four data sets named
SCA3, SCA8, CON3, and CON8. Each data set consists of 10 instances
18 50-customer problem with specific characteristics: SCA data sets
are g 18 lated with customers scattered uniformly in the service region, CON data sets are generated with half of the customers located
uniformly in the service region and the other half are concentrated
in certain 70 t of the service region. The number after SCA or CON
indicated the parameter for determining vehicle capacity.

18 As mentioned earlier, the VRPSPD is formulated by Dethloff [4] as the problem to minimize the total traveled distance subject to 18 kimum capacity constraint of the vehicle. Hence, the following 18 blem parameters are set as follows: fixed cost per vehicle, f = 0; var 3 le cost per distance unit, g = 1; service duration limit $D = \infty$; and the num 60 of available vehicles is equal to the number of available vehicle 4 the best known solution.

The comparison of the best solution among 10 PSO iterations with the result from Dethloff [4], Tang and Galvao [7] and Bianchessi and Righini [8] is presented in Table 3. To make a direct comparison across these existing results, only the average result over the 10 instances of each data set is reported. It is shown that the proposed

Table 3Comparison of several methods on Dethloff data.

Set	Average total cost						
	Dethloff [4]	Tang and Galvao [7]	Bianchessi and Righini [8]	PSO			
SCA3	746.6	674.2	684.6	675.8 ^{a,c}			
SCA8	1166.4	1044.4	1035.7	1041.8a,b			
CON3	597.3	564.2	568.5	569.6a			
CON8	860.6	774.3	776.4	798.3a			

^aPSO result better than Dethloff result.

bPSO result better than Tang and Galvao result.

^cPSO result better than Bianchessi and Righini result.

PSO method is competitive wi 71 xisting methods: the PSO result outperforms the Dg ploff result for all data set, better than the Tang and Galvao result for SCA8 data set, and better than the Bianchessi and Righini result for SCA3 data set. More over, only small difference between PSO and the best result is observed for other cases. In addition to this result, the proposed PSO gives a reasonable computational time for solving this benchmark data in which approximately only 30 s of computational time is required for each instance.

4.1.3. Nagy and Salhi data

Another computational experiment is conducted by applying this proposed algorithm to the benchmark data set of Nagy and Salhi [6] which modified the basic VRP benchmark data set of Christofides 7 to be the benchmark data set of VRPSPD. The corresponding 7 pot and customer coordinate remained the same, but the original delivery demand data on basic VRP benchmark is split into pickup quantity and delivery quantity. There are five new sets of data based on 46 plitting method of demand data, and the new problem sets are named *T. Q. H. X.*, and *Y*.

Since the proposed method is implemented for the general formulation of VRPSPD, problem parameters need to be set in order to compare with results frog previous works of VRPSPD. The following 4 oblem parameters are used: fixed cost per vehicle, f=0; variable cost per distance unit, g=1; traveling time is equal to correspondage traveled distance, $t_{ij}=d_{ij}$; and the number of available vehicles is equal to the number of a a_{ij} able vehicle in the best known solution. The result of problem f, g, and g are compared with the best results from Salhi and Nagy [5], which is the only result found in the literature. The result of problem g and g are compared with the best solution among Nagy and Salhi [6], Dethloff [4], Tang and Galvao [7]. However, result of Tang and Galvao [7] for instances number 6–10 and 13–14 are omitted from comparison because the different problem g ting in which the customer service time are not considered.

In ord 32 o compare the solution obtained with the best-known solu 32, percentage of deviation from best-known solution is used. The formula for calculating the percentage of deviation is as follows:

$$\%dev = \frac{Z - Z*}{Z*} \times 100\%$$
(22)

Solution: 32

Solution: 2:

61 ere % dev: percentage of deviation from best-known solution; Z: objective function of current solution; Z*: objective function of best known 41 ution.

48 The comparison of the best solution among 10 PSO iterations 32 the best-known solutions are shown in Tables 4 and 5. This comparison shows that the results from the proposed PSO algorithm are competitive with other published results. As shown in Table 4, in almost all instances of the problem *T*, *Q*, and *H*, the best objective function of PSO results are better than the corresponding best-known solutions. Additionally from Table 5, the PSO result of sixteen instances of problem *X* and *Y* are better than its corresponding best-known solution. The detail of these new best solutions of VRPSPD instances are presented in the following webpage:

19 I.J. Ai, V. Kachitvichyanukul / Computers & Operations Research 36 (2009) 1693 – 1702

4 ble 4 Comparison of best-known solution and best PSO solution of T, Q and H Instances with fixed cost f = 0 and variable cost g = 1.

Instance	Best-kr	nown solution [5]	Best PS	O solution	
	No. vel	hicle Total cost (distance)	No. veh	nicle Total cost (distance)	% dev
CMT1T	5	541	5	520	-3.9
CMT2T	10	839	9	810	-3.5
CMT3T	10	903	7	827	-8.5
CMT4T	13	1111	11	1014	-8.8
CMT5T	18	1423	15	1297	-8.9
24 6T	6	571	6	555	-2.7
CMT7T		-	12	942	-
CMT8T	10	911	9	904	-0.7
CMT9T	14	1164	14	1206	3.6
CMT10T	18	1418	18	1501	5.8
CMT11T	7	1075	7	1026	-4.5
CMT12T	10	827	9	792	-4.3
CMT13T	12	1600	11	1548	-3.3
CMT14T	11	866	10	846	-2.3
CMT1Q	5	557	4	490	-12.1
CMT2Q	11	860	8	739	-14.1
CMT3Q	9	918	6	768	-16.4
CMT4Q	14	1164	9	938	-19.4
CMT5Q	19	1477	13	1174	-20.5
CMT6Q	6	594	6	557	-6.3
CMT7Q	-		12	933	
CMT8Q	9	918	9	890	-3.0
CMT9Q	15	1178	14	1214	3.1
CMT10Q	19	1477	18	1509	2.2
CMT11Q	7	1075	6	964	-10.3
CMT12Q	10	843	7	733	-13.1
CMT13Q	13	1613	11	1570	-2.7
CMT14Q	11	873	10	825	-5.5
CMT1H	6	594	3	464	-21.8
CMT2H	12	873	6	668	-23.4
СМТ3Н	9	915	4	701	-23.4
CMT4H	14	1164	6	883	-24.1
CMT5H	19	1509	9	1044	-30.8
CMT6H	6	594	6	557	-6.3
CMT7H	-	-	11	943	-
CMT8H	9	915	9	899	-1.7
СМТ9Н	14	1164	14	1207	3.7
CMT10H	19	1509	19	1499	-0.7
CMT11H	8	1120	4	830	-25.9
CMT12H	11	850	5	635	-25.3
CMT13H	11	1546	11	1565	1.2
CMT14H	11	866	10	824	-4.8

http://ind.uajy.ac.id/~jinai/PSQ 41; _VRPSPD_COR_Appendix.htm. Furthermore, for all instances that are worse than the best-known solution, the biggest deviation is about six percent.

Statistics of the PSO result on prob 4 ns X and Y are presented in

Statistics of the PSO result on prob 4 is X and Y are presented in Table 6. It comprises the average and standard deviation of the objective function, percentage of standard deviation over the average, and the 69 age computational time. The robustness of the proposed method in term of solution q 16 by is implied in this statistics. Even though t 16 proposed method is a random search algorithm, the variation of solutions over replications are very consistent as demonstrated by the small standard devia 8 h.

The computational results show that the computational time of the proposed method tends to be linearly proportional with the number of customers, which is representing the problem size. This relation is desirable, since it is only require linear additional time to apply to method on a bigger size problem.

The high-quality result yielded by the proposed method might come from two factors: the idea of vehicle orientation and the heuristic for constructing routes. The implementation of vehicle orientation will ensure the span closeness of customers that are included in the route. Hence, the constructed route will cover only a relatively narrow area. The customer is inserted into the best position in an existing route by applying the route construction heuristics. Furthermore, the 2-opt method is capable of improving a newly constructed

4 ble 5 Comparison of best-known solution and best PSO solution of X and Y instances with fixed cost f = 0 and variable cost g = 1.

Instance	Best-kno	own solution		Best PS0) solution	
	No. vehicle	Total cost (distance)	Ref.	No. vehicle	Total cost (distance)	% dev
CMT1X	3	472	[7]	3	467	-1.1
CMT1Y	3	470	[7]	3	467	-0.7
CMT2X	7	695	[7]	6	710	2.1
CMT2Y	7	700	[7]	6	710	1.5
CMT3X	5	721	[7]	5	738	2.3
CMT3Y	5	719	[7]	5	740	3.0
CMT4X	7	880	[7]	7	912	3.7
CMT4Y	7	878	[7]	7	913	4.0
CMT5X	11	1098	[7]	10	1167	6.3
CMT5Y	10	1083	[7]	10	1142	5.5
CMT6X	6	584	[4]	6	557	-4.7
CMT6Y	6	584	[4]	6	557	-4.7
CMT7X	11	961	[4]	11	919	-4.3
CMT7Y	11	961	[4]	11	934	-2.8
CMT8X	10	923	[5]	9	896	-2.9
CMT8Y	10	923	[5]	9	902	-2.3
CMT9X	15	1215	[5]	15	1225	0.8
CMT9Y	15	1215	[5]	15	1230	1.3
CMT10X	19	1571	[4]	19	1520	-3.3
CMT10Y	20	1527	[4]	18	1485	-2.8
CMT11X	4	900	[7]	4	895	-0.5
CMT11Y	5	910	[7]	4	900	-1.1
CMT12X	6	675	[7]	5	691	2.4
CMT12Y	6	689	[7]	5	697	1.2
CMT13X	11	1576	[4]	11	1560	-1.0
CMT13Y	11	1576	[4]	11	1568	-0.5
CMT14X	10	871	[4]	10	826	-5.2
CMT14Y	10	871	[4]	10	823	-5.5

Table 6Statistical summary of PSO result on *X* and *Y* instances.

Instance No	. cust. Average total cost	Standa deviati		
CMT1X 2	4 469.57	2.95	0.6	40
CMT1Y 5		2.77	0.6	40
CMT2X 7	717.45	6.85	1.0	54
CMT2Y 7	5 716.70	5.13	0.7	54
CMT3X 10	746.20	4.08	0.5	114
CMT3Y 10	0 746.78	3.76	0.5	113
CMT4X 15	928.20	7.98	0.9	207
CMT4Y 15	0 926.12	6.75	0.7	204
CMT5X 19	9 1196.13	17.39	1.5	285
CMT5Y 19	9 1182.67	22.74	1.9	286
CMT6X 5	558.53	1.02	0.2	28
CMT6Y 5	0 559.12	1.03	0.2	28
CMT7X 7	944.13	17.80	1.9	66
CMT7Y 7	5 956.90	15.01	1.6	65
CMT8X 10	912.87	10.69	1.2	99
CMT8Y 10	0 918.56	10.27	1.1	100
CMT9X 15	0 1246.24	10.95	0.9	189
CMT9Y 15	0 1245.14	14.31	1.1	187
CMT10X 19	9 1529.45	6.28	0.4	323
CMT10Y 19	9 1516.23	22.09	1.5	323
CMT11X 12	915.30	15.69	1.7	226
CMT11Y 12	0 913.77	10.53	1.2	228
CMT12X 10	716.80	24.75	3.5	115
CMT12Y 10		25.18	3.5	114
CMT13X 12	0 1575.61	10.48	0.7	135
CMT13Y 12		7.89	0.5	135
CMT14X 10		4.84	0.6	98
CMT14Y 10	0 829.93	5.25	0.6	97

route. The combinations of these efforts are potential for yielding a good solution.

The simplicity of PSO may also contribute to the performance. By its mechanism, the particles are able to explore various areas in the searching space within a few computational steps. It means that diverse solutions of vehicle routes are generated during the iteration process, since one particle corresponds to one solution of vehicle routes. This diversification of solutions will increase the possibility

7 ble 7 Comparison of best-known solution and best PSO solution of *X* and *Y* instances with fixed cost f = 100 and variable cost g = 1.

Instance	Best-kno	wn solutio	n		Best PSC	solution		
	No. vehicle	Total distance	Total cost	Ref.	No. vehicle	Total distance	Total cost	% dev
CMT1X	3	472	772	[7]	3	467	767	-0.7
CMT1Y	3	470	770	[7]	3	467	767	-0.4
CMT2X	7	695	1395	[7]	6	707	1307	-6.3
CMT2Y	7	700	1400	[7]	6	709	1309	-6.5
CMT3X	5	721	1221	[7]	5	742	1242	1.7
CMT3Y	5	719	1219	[7]	5	739	1239	1.7
CMT4X	7	880	1580	[7]	7	923	1623	2.7
CMT4Y	7	878	1578	[7]	7	920	1620	2.7
CMT5X	11	1098	2198	[7]	10	1150	2150	-2.2
CMT5Y	10	1083	2083	[7]	10	1138	2138	2.7
CMT6X	6	584	1184	[4]	6	557	1157	-2.3
CMT6Y	6	584	1184	[4]	6	557	1157	-2.3
CMT7X	11	961	2061	[4]	11	931	2031	-1.4
CMT7Y	11	961	2061	[4]	11	933	2033	-1.4
CMT8X	9	928	1828	[4]	9	902	1802	-1.4
CMT8Y	9	936	1836	[4]	9	906	1806	-1.6
CMT9X	15	1215	2715	[5]	15	1229	2729	0.5
CMT9Y	15	1215	2715	[5]	15	1237	2737	0.8
CMT10X	19	1571	3471	[4]	19	1499	3399	-2.1
CMT10Y	19	1571	3471	[4]	19	1485	3385	-2.5
CMT11X	4	900	1300	[7]	4	898	1298	-0.2
CMT11Y	5	910	1410	[7]	4	904	1304	-7.5
CMT12X	6	675	1275	[7]	5	682	1182	-7.3
CMT12Y	6	689	1289	[7]	5	681	1181	-8.4
CMT13X	11	1576	2676	[4]	11	1570	2670	-0.2
CMT13Y	11	1576	2676	[4]	11	1568	2668	-0.3
CMT14X	10	871	1871	[4]	10	824	1824	-2.5
CMT14Y	10	871	1871	[4]	10	824	1824	-2.5

to find a high-quality solution. In addition, the searching mechanism of the particle also fits for searching the vehicle orientations, in which the best point of a vehicle orientation is explored around current best points. Furthermore, PSO always keeps and uses the information on the best position of the particles to direct the particles 159 ement. Consequently, the iteration process of PSO may end with a high-quality solution within a relatively short computational time.

4.2. Effect of fixed cost

The computational results in Section 4.1 are inline with the previous work in VRPSPD, in which ignoring the fixed cost of vehicle. However, literature on other areas of VRP have acknowledged the importance of the fixed cost of vehicle and considered it as one part of the objective function [1]. The proposed method can straightforwardly handle this situation, since the mathematical model considered the fix 54 ost in the objective function.

Another computational experiment is carried out in order to show the performance of the proposed method when considering fixed cost. All PSO and problem parameters are the same as those used in the experiment in Section 4.1.3, except that the fixed cost is set as 100. The result of this experiment for problems X and Y are shown in Table 7. For comparison purpose, the total cost of the best result previous works [4,5,7] are recalculated using similar unit cost of fixed cost f = 100 and variable cost g = 1 before to be selected as the best-known solution.

It is shown in Table 7 that the computational PSO result for 21 instances of problems *X* and *Y* are better than the best-known solution. By using this amount of fixed cost, it implies that the smaller number 33 ehicles leads to the better total cost. Hence, it is not a surprise that the proposed method result is frequently better than the best-known solution since a special effort for reducing the number of vehicles (Algorithm 3) is included. This effort will ensure that the number of vehicles is as small as possible. As a result, the

number of vehicles from the PSO result is at most exactly the same as the best-known solution and in some cases smaller than those of the best-known solutions.

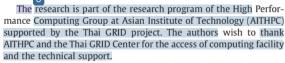
5. Conclusion and further study

A generalized formu 430n of VRPSPD for three existing formulations in the literature is presented in this paper along with a solution 25 hod based on PSO algorithm. The computational result shows that the proposed PSO method is effective for solving the VRPSPD. The effectiveness of the method comes from the combination of following reasons. First, the idea of vehi 5 orientation makes each of routes only cover a 26 tricted area. Second, the solution quality is improved from the cheapest insertion heuristic and 2-opt method which are applie 41 uring the route construction. Third, a special algorithm reduces t 25 umber of vehicles that actually serve the customers. Fourth, the mechanism of PSO that can generate diverse solutions and keep the best solution found during the iteration profits.

Some aspects may further improve the performance of the proposed algorithm, such as parameter optimization and programming implementation. Although the PSO parameter set used in this paper [1] from some preliminary experiment, it may not be the best one. In addition, the programming implementation of the algorithm may be further optimized. Since these efforts may yet contribute to additional performance gains in both the solution quality and computational time, a further study on these aspects is still necessary.

Some further research to apply the proposed method to other VRP variants should be carried out to show generality of the method. Since the variants of VRP differ from one another only on the specific problem constraints, the adjustment is only required in the constraint feasibility checking of the decoding method. However, the effectiveness of this idea needs further exploration.

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