



Search within this journal

Search

[Home](#) / [Archives](#) / Vol 7 No 2 (2018)

## Articles

### [A Distance-Reduction Trajectory Tracking Control Algorithm for a Rear-Steered AGV](#)

Anugrah K Pamosoaji

75-90 | published: 2018-06-11

### [Localization of Leader-Follower Robot Using Extended Kalman Filter](#)

Siti Nurmaini, Sahat Pangidoan

91-104 | published: 2018-06-11

### [Swarm Intelligent in Bio-Inspired Perspective: A Summary](#)

Nyayu Husni Latifah, Ade Silvia, Ekawati Prihatini, Siti Nurmaini, Irsyadi Yani

105-120 | published: 2018-06-11

### [Detection of Vessel on UAV based on Segmentation Using Edge Based Dilation](#)

Muhammad Khaerul Naim Mursalim, Noor Falih

121-128 | published: 2018-06-11

### [Quantitative Evaluation on Electric Motor Thermal Image for Comparison Hot Spot and Measuring Point Regions](#)

Wa Ode Siti Nur Alam, Sahabuddin Hay, St Nawal Jaya

129-136 | published: 2018-06-11

### [Study of Molecular Docking of Chalcone Analogue Compound as Inhibitors for Liver Cancer Cells HepG2](#)

Neni Frimayanti, Enda Mora, Rizki Anugrah

137-147 | published: 2018-06-11



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## A Distance-Reduction Trajectory Tracking Control Algorithm for a Rear-Steered AGV

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### ABSTRACT

This paper presents a Lyapunov-based switched trajectory tracking control design for a rear-steered automated guided AGV (AGV). Given a moving reference whose position and orientation have to be tracked by the AGV, the main objective of the controller is to reduce AGV's distance from the reference while adjusting its orientation. The distance reduction issue is important, especially in huge warehouses operating a group of AGVs, since the rate of AGV-to-reference distance reduction contributes to the possibility of AGV-to-AGV collision. A set of control algorithms is proposed to handle large AGV's orientation. Simulations that show the performance of the proposed method is presented.

**Keywords:** Tracking control, automated guided AGV, distance reduction, collision avoidance.

### 1. INTRODUCTION

Trajectory tracking for AGVs has been studied for decades. This issue becomes important when an AGV groups start to operate in a large workspace, such as warehouse. Here, one of the aspects of a warehouse is order-picking mechanism [1]. In association with the use of AGVs, warehouse management area mostly discusses about mechanism to generate AGV trajectory plan [2-4]. In robotics, the realizations of the plan have been addressed under a typical terminology, i.e., "trajectory tracking".

A huge number of tracking strategies have been developed. Roughly speaking, developments of tracking algorithm for AGVs can be divided into two directions: first, path tracking which focused on the placement of a physical AGV to a planned path. Research on this issue was established in [5-9]. The second type of this study is trajectory tracking, which is focused on the placement of physical AGV to the reference at any time instance. Several works applied Cartesian coordinate system to express the AGV's configuration [10-12]. Such the type of methods has a complexity in controlling AGV-to- target distance that is necessary especially for the problem of tracking moving preplanned references in multiple AGV systems.

Inter-AGV collision avoidance has been an interesting issue. Various approaches to this problem have been proposed. They can be categorized according to two paradigms: those involving communication among the AGVs in a group, and those with no such communication. In the first paradigm, the communication among AGVs became an important consideration regarding to performance of decentralized control and coordination [5-10]. In [6], the problem of conflict resolution for multiple AGVs was treated, focusing on the goal reachability and safety guarantee. In this approach, right-turn-only policy was followed. In [7], decentralized navigation of groups of nonholonomic wheeled mobile robots was proposed.

Maintenance of inter-robot distances while the leader moved along collision-avoidance trajectories was focused. In line with [6], the work in [8] proposed an approach named Resource Allocation Systems for free-ranging multiAGV systems. Bekris et al. investigated the coordination of the motions of second-order robots in consideration of planning-cycle differences [10].

A plan in warehouse management is a good plan if it is trackable in a finite time. The tractability of the plan is indicated by the ability of the controller to reduce the distance between the AGV and the plan. This problem can be solved by, first, using a polar coordinate system, since one of its axis can represent such the distance. Some trajectory tracking controls using polar coordinate system are reported in [12-18]. The works in [17] and [18], for instance, proposed a class of model predictive control for trajectory tracking. In [14], an error-based control for robust trajectory tracking for unmanned ground AGVs.

However, most publications lack of concerning the reducing AGV-to-reference distance under extreme AGV's orientation. This issue is important, since mostly, at the beginning the initial configuration of the AGV is not the same with the plan. Moreover, it is possible that the AGV starts to track the assigned plan from extreme orientation in polar coordinate system. If the AGV disable to track the plan, under a crowded circumstance, it is possible that a collision between the AGV to another single one is inevitable.

In this paper, a control algorithm is designed to drive a rear-steered AGV to its respective reference focusing on decreasing distance between the AGV and the reference. The contribution of this study is twofold: first, the design of controller to minimize collision to other AGVs with their own plans. Second, the controller answers question of reducing AGV-to-reference distance even the initial navigation angles are extreme.

The organization of this paper is as follows. Section 2 describes the problem definition; Section 3 explains the proposed controller design; Section 4 presents the simulation results; and Section 5 concludes this paper.

## 2. PROBLEM DEFINITION

Suppose that there exists a rear-steered AGV whose location is represented by the coordinate  $(x, y)$  and orientation by  $\delta$  as shown in Figure1. The AGV has to drive its controlled point  $P$  with traction velocity  $u$  and angular velocity  $\omega$ ;  $l$  represents the distance between the centers of actuation  $O$ . The AGV itself has two actuators, i.e., velocity  $v$  and steering  $\delta$ . The kinematic model of the AGV is given as

$$\dot{x} = v \cos \theta \cos \delta \quad (1)$$

$$\dot{y} = v \sin \theta \cos \delta \quad (2)$$

$$\dot{\theta} = -(v/l) \sin \delta \quad (3)$$

The AGV has to track a reference whose location is represented by  $(x_r, y_r)$  and orientation by  $\theta_r$ , as shown in Figure2. Our assumption is that the configuration

(velocity and orientation) of the reference is predefined and is represented by its traction and angular velocities, i.e.,  $v_r$  and  $\omega_r$ , respectively.

For tracking control design purpose, we define navigation variables  $(\rho, \alpha, \varphi)$  formulated as

$$\rho = \sqrt{\Delta x^2 + \Delta y^2} \quad (4)$$

$$\alpha = \arctan2(\Delta y, \Delta x) - \theta \quad (5)$$

$$\varphi = \theta_g - \arctan2(\Delta y, \Delta x) \quad (6)$$

where  $\Delta x = x_r - x$ ,  $\Delta y = y_r - y$ . In this paper, we address a problem of trajectory tracking control for extreme navigation angles  $\alpha$  and  $\varphi$ , i.e., at least one of the following conditions occurs:

$$\pi/2 < \alpha \leq \pi \cup -\pi < \alpha < -\pi/2 \quad (7)$$

$$\pi/2 < \varphi \leq \pi \cup -\pi < \varphi < -\pi/2 \quad (8)$$

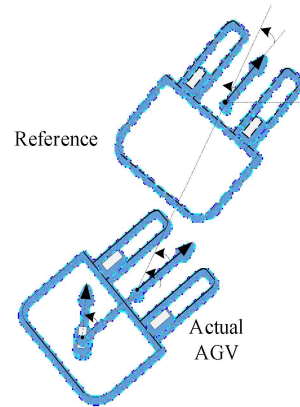
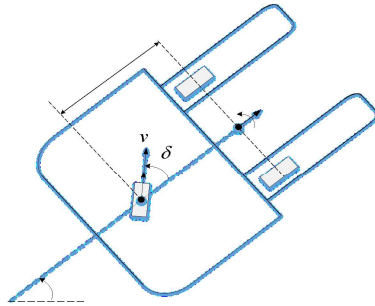


FIGURE 1. Kinematic model of an AGV

FIGURE 2. Trajectory tracking scenario

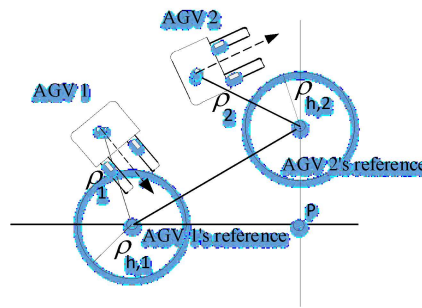


FIGURE 3. Multiple-AGV trajectory tracking problem near a conflict point

**Anugrah K. Pamosoaji**  
**A Distance-Reduction Trajectory Tracking Control Algorithm**  
**for a Rear-Steered AGV**

The situation to address is shown in Figure3. Suppose that two AGVs follow their own plan (reference) and assume that their plans have intersection at point  $P$ . Assume that the plan is predefined such that if each AGV occupies the desired trajectory, inter-AGV collision can be avoided. Therefore, a control mechanism must be designed to reach the collision-free motion. However, since the AGVs are nonholomic, the orientations of the AGVs contribute to the motion. In most cases, initial orientation sometimes prohibits the AGV to decrease the AGV-to-AGV distance.

The extreme initial navigation angles appears in [14-15] for point stabilization problem. In the problem, the control law has no effect of reference's velocities since its velocities are zero. However, for the case of moving reference, the reference's motion influences the evolution of navigation variables in Equations (4)-(6).

The evolution of the navigation variables is described as follows.

$$\dot{q}(t) = f(q), q(0) = q_0 \quad (9)$$

where

$$f = \begin{bmatrix} v_r \cos \phi - v \cos \alpha \cos \delta \\ -v_r / \rho \sin \phi + v / \rho \sin \alpha \cos \delta + v_r / l \sin \delta \\ v_r / \rho \sin \phi - v / \rho \sin \alpha \cos \delta + \omega_r \end{bmatrix} \quad (10)$$

$$q(t) = [\rho \quad \alpha \quad \varphi]^T \quad (11)$$

The objective of this paper is twofold. First is to design a trajectory tracking algorithm such that

$$\lim_{t \rightarrow \infty} \rho \leq \rho_{ss} \quad (12)$$

$$\lim_{t \rightarrow \infty} \alpha \approx 0, \quad (13)$$

$$\lim_{t \rightarrow \infty} \varphi \approx 0, \quad (14)$$

where  $t$  represents time and  $\rho_{ss}$  is maximum steady-state distance. Second, the paper identifies necessary and sufficient conditions such that the distance is kept decrease.

The dynamics of the actuator is derived by the following steps. Note that the parameters used in the dynamics are described in Table 1. The torques applied to the driving and steering motors are formulated as

$$\tau_{dr} = I_{dr} \dot{\omega}_{dr} + B_{dr} \omega_{dr} + F_{dr} r_{dr}. \quad (15)$$

$$\tau_{\delta} = I_{\delta} \dot{\omega}_{\delta} + B_{\delta} \omega_{\delta} \quad (16)$$

TABLE 1.  
Dynamics symbols and definitions

Symbol	Definition
$\tau_{dr}$ and $\tau_{\delta}$	Torque produced by the driving and steering motors, respectively.
$F_{dr}$	Traction force applied to the driving motor.
$I_{dr}$ and $I_{\delta}$	Moment of inertia of the driving wheel controlled by the driving and steering motors, respectively.
$\omega_{dr}$ and $\omega_{\delta}$	angular velocity of the driving and steering motors, respectively.
$B_{dr}$ and $B_{\delta}$	viscous friction coefficient of the driving and steering motors, respectively.
$r_{dr}$	radius of the driving wheel.
$k_{a, dr}$ and $k_{a, \delta}$	torque constant of the driving and steering motors, respectively.
$k_{b, dr}$ and $k_{b, \delta}$	voltage constant of the driving and steering motors, respectively.
$R_{dr}$ and $R_{\delta}$	electric resistance constants of the driving and steering motors, respectively.
$u_v$ and $u_{\delta}$	input voltage applied to the driving and steering motors, respectively.

The model of driving and steering motors are described as

$$\tau_{dr} = (k_{a, dr}(u_v - k_{b, dr}\omega_{dr}))/R_{dr}, \quad (17)$$

$$\tau_{\delta} = (k_{a, \delta}(u_{\delta} - k_{b, \delta}\omega_{\delta}))/R_{\delta}. \quad (18)$$

Substitute Equation (17) to Equation (15) yields

$$\frac{I_{dr}R_{dr}}{k_{a, dr}}\dot{\omega}_{dr} + \left(\frac{B_{dr}R_{dr} + k_{a, dr}k_{b, dr}}{k_{a, dr}}\right)\omega_{dr} + F_{dr}R_{dr}r_{dr} = k_{P, v}(\dot{v}_{dr} - v_{dr}) - k_{D, v}\dot{v}_{dr}. \quad (19)$$

Since  $\omega_{dr} = \frac{v_{dr}}{r_{dr}}$ , then Equation (19) is rewritten as

$$F_{dr}R_{dr}r_{dr}^2 = k_{P, v}r_{dr}v_{dr}^* - \left(k_{D, v}r_{dr} + \frac{I_{dr}R_{dr}}{k_{a, dr}}\right)\dot{v}_{dr} - \left(\frac{B_{dr}R_{dr} + k_{a, dr}k_{b, dr}}{k_{a, dr}} + k_{P, v}r_{dr}\right)v_{dr} \quad (20)$$

where  $v_{dr}^*$  is the planned driving velocity of the AGV. Since  $F_{dr} = I_{dr} \frac{\dot{v}_{dr}}{r_{dr}}$ , then

Equation (20) is rewritten as

$$\left( k_{D,v} r_{dr} + \left( \frac{1}{k_{a,dr}} + r_{dr} \right) I_{dr} R_{dr} \right) \dot{v}_{dr} + \left( \frac{B_{dr} R_{dr} + k_{a,dr} k_{b,dr}}{k_{a,dr}} + k_{P,v} r_{dr} \right) v_{dr} - k_{P,v} r_{dr} v_{dr}^* = 0 \quad (21)$$

Substitution of (18) to (16) yields

$$\frac{I_{\delta} R_{\delta}}{k_{a,\delta}} \dot{\omega}_{\delta} + \left( \frac{B_{\delta} R_{\delta} + k_{a,\delta} k_{b,\delta}}{k_{a,\delta}} \right) \omega_{\delta} = k_{P,\delta} (\delta^* - \delta) - k_{D,\delta} \dot{\delta} \quad (22)$$

where  $\delta^*$  is the planned steering angle of the AGV. Time derivative of (22) is

$$\frac{I_{\delta} R_{\delta}}{k_{a,\delta}} \ddot{\omega}_{\delta} + \left( \frac{B_{\delta} R_{\delta} + k_{a,\delta} k_{b,\delta}}{k_{a,\delta}} + k_{D,\delta} \right) \dot{\omega}_{\delta} - k_{P,\delta} (\dot{\omega}_{\delta}^* - \dot{\omega}_{\delta}) = 0 \quad (23)$$

### 3. CONTROL DESIGN

A control algorithm is designed to accommodate extreme configuration. The proposed control is Lyapunov-based control which consists of two parts, i.e., distance reduction and orientation controls.

#### 2.1 DISTANCE-REDUCTION CONTROL

The purpose of distance control is to drive the AGV such that Equation (12) is satisfied. For this type of control, we propose switched traction velocity control, as explained in Propositions 2 and 3. The idea is in this control, we regard only one actuator, i.e.,  $v$  and the other one, i.e., steering actuator  $\delta$  as a parameter.

*Proposition 1:* The following properties lead to  $\dot{\rho} < 0$ :

$$1) v \cos \alpha > 0. \quad (24)$$

$$2) v \cos \alpha < 0 \text{ and } v_r \cos \varphi < v \cos \alpha. \quad (25)$$

*Proof:* Suppose that  $\dot{\rho} < 0$ . The first equation of Equation (10) can be rewritten as

$$v_r \cos \varphi - v \cos \alpha \cos \delta = w, \quad (26)$$

where  $w < 0$ . (26) can be rewritten as

$$\cos \delta = \frac{-w + v_r \cos \varphi}{v \cos \alpha}. \quad (27)$$

Since  $0 \leq \cos \delta \leq 1$ , then the value of the right side of (27) must be in the interval of  $[0, 1]$ . In other words,  $0 \leq (-w + v_r \cos \varphi)(v \cos \alpha)^{-1} \leq 1$ . Suppose that  $v \cos \alpha > 0$  and  $v_r \cos \varphi \geq 0$ . Then we have the following admissible range of  $w$ .

$$v_r \cos \varphi \geq w \geq -v \cos \alpha + v_r \cos \varphi \quad (28)$$

It is clear that  $v_r \cos \varphi - v \cos \alpha < \dot{\rho} < 0$ , which confirms that the lower bound of  $w$  is negative. In addition, since  $v_r \cos \varphi \geq 0$ , the upper bound of  $w$  is zero to satisfy (26). Therefore,  $w$  spans in the interval  $-v \cos \alpha + v_r \cos \varphi \leq w \leq 0$ . For  $v \cos \alpha > 0$



and  $v_r \cos \varphi \leq 0$ , the admissible range of  $w$  is the same with (28). Since the upper bound of  $w$  is negative, then in this condition  $\dot{\rho}$  is always negative.

The next case is when  $v \cos \alpha < 0$  and  $v_r \cos \varphi \geq 0$ . In this situation, we have the following admissible range of  $w$ .

$$v_r \cos \varphi \leq w \leq -v \cos \alpha + v_r \cos \varphi. \quad (29)$$

Since the lower and upper bounds of  $w$  is non-negative, we can conclude that  $\dot{\rho}$  is always positive in this condition. The last condition to check is when  $v \cos \alpha < 0$  and  $v_r \cos \varphi < 0$ . The admissible range of  $w$  is in the same form with Equation (29). Hence, the upper bound of  $w$  would be negative if and only if  $v_r \cos \varphi < v \cos \alpha$ .

*Proposition 2:* Suppose that  $\cos \delta > 0$ . Define  $\psi = \cos \alpha \cos \delta$ . For  $v_r \cos \varphi < 0$ , the following traction velocity control.

$$v = -k_{v,1} \text{sgn}(\psi) |v_r \cos \varphi \psi^{-1}| \quad (30)$$

where  $0 < k_{v,1} < 1$  is a constant, makes the AGV-to-reference  $\rho$  closer to zero.

*Proof:* Define a Lyapunov candidate function

$$V_1 = 0.5 k_\rho \rho^2. \quad (31)$$

The first time derivative of  $V_1$  is

$$\dot{V}_1 = k_\rho \rho \dot{\rho}. \quad (32)$$

Substitution of Equation (11) to Equation (32) yields

$$\dot{V}_1 = -k_\rho \rho v \psi + k_\rho \rho v_r \cos \varphi \quad (33)$$

The AGV-to-reference  $\rho$  tends to zero if  $\dot{V}_1 < 0$ . Under the condition of  $v_r \cos \varphi < 0$  and  $\psi < 0$ , the substitution of Equation (30) to Equation (33) yields  $\dot{V}_1 = -(1 - k_{v,1}) k_\rho \rho |v_r \cos \varphi|$ , which can be less than zero if and only if  $0 < k_{v,1} < 1$ . The similar analysis for  $v_r \cos \varphi < 0$  and  $\psi > 0$  yields  $\dot{V}_1 = (k_{v,1} - 1) k_\rho \rho |v_r \cos \varphi|$ , which leads to  $\dot{V}_1 < 0$  if  $0 < k_{v,1} < 1$ .

*Proposition 3:* Suppose that  $\cos \delta > 0$ . For  $v_r \cos \varphi > 0$ , the following traction velocity control

$$v = k_{v,2} \text{sgn}(\psi) (|v_r \cos \varphi \psi^{-1}| + \bar{v}), \quad (34)$$

where

$$k_{v,2} > (1 + |\psi| \bar{v} / |v_r \cos \varphi|)^{-1} \quad (35)$$

is a constant, makes the AGV-to-reference  $\rho$  closer to zero.

*Proof:* The proof can be made by using the same Lyapunov candidate function in Proposition 2. Under the condition of  $v_r \cos \varphi > 0$  and  $\psi < 0$ , the substitution of Equation (34) to Equation (33) yields  $\dot{V}_1 = k_\rho \rho (v_r \cos \varphi - k_{v,2} (v_r \cos \varphi + |\psi| \bar{v}))$ , which is negative definite if  $k_{v,2}$  satisfies Equation (35). The same result can be obtained for the other condition, i.e.,  $v_r \cos \varphi > 0$  and  $\psi > 0$ .

## 2.2 ORIENTATION CONTROL

The purpose of orientation control is to drive the AGV such that Equations (13)-(14) is satisfied. Here, as explained in Propositions 4 and 5, we regard  $\delta$  as the actuator and  $v$  as a parameter. Define a constant  $\lambda > 0$  and a coefficient  $k_{v,3}$  that describes the relation between  $v$  and  $v_r$  as follows.

$$v_r \sin \varphi = k_{v,3} v \sin \alpha \quad (36)$$

In addition, define

$$\cos \delta = \begin{cases} (1 - h^2)^{1/2}, & \text{if } \delta \in [-\pi/2, \pi/2] \\ -(1 - h^2)^{1/2}, & \text{otherwise,} \end{cases} \quad (37)$$

$$\sin \delta = \begin{cases} h, & \text{if } \delta \in [0, \pi] \\ -h, & \text{otherwise,} \end{cases} \quad (38)$$

and  $h \in [0, 1]$ .

Define another Lyapunov candidate function

$$V_2 = 0.5 k_\rho (\alpha^2 + \varphi^2), \quad (39)$$

where  $k_\rho > 0$  is constant. The first time derivative of  $V_2$  is

$$\dot{V}_2 = \dot{V}_{21} + \dot{V}_{22}. \quad (40)$$

where

$$\dot{V}_{21} = (v_r \sin \varphi - v \sin \alpha \cos \delta) (\varphi - \alpha) / \rho \quad (41)$$

$$\dot{V}_{22} = (\alpha v / l) \sin \delta + \varphi \omega^r \quad (42)$$

We can state the following proposition.

*Proposition 4:* The following steering control

$$\delta = \begin{cases} \tan^{-1} \gamma_1, & \text{if } h / \sqrt{1 - h^2} \geq 0, \\ -\tan^{-1} \gamma_1, & \text{otherwise,} \end{cases} \quad (43)$$

where  $\gamma_1 = \sqrt{(k_{v,3} + \lambda_{12} \rho v \sin \alpha (\varphi - \alpha))^{-2} - 1}$ ,  $\lambda_1 > 0$ , and  $k_{v,3} > 0$ , drives  $\alpha$  and  $\varphi$  to zero, under the necessary condition of

$$(k_{v,3} + \lambda_{12} \rho v \sin \alpha (\varphi - \alpha))^2 \leq 1 \quad (44)$$

*Proof:* We have to proof that  $\dot{V}_{21} \leq 0$  for all  $\dot{V}_{21} = (v_r \sin \varphi - v \sin \alpha \cos \delta) (\varphi - \alpha) / \rho$ ,  $\alpha \in [-\pi, \pi]$  and  $\varphi \in [-\pi, \pi]$ . Substitution of Equation (37) to Equation (41) yields

$$\dot{V}_{21} = (v_r \sin \varphi - v \sin \alpha \sqrt{1 - h^2}) (\varphi - \alpha) / \rho. \quad (45)$$

Therefore Equation (45) can be rewritten as

$$\dot{V}_{21} = (k_{v,3} - (1 - h^2)^{1/2}) v \sin \alpha (\varphi - \alpha) / \rho \quad (46)$$

Define  $h$  as follows.

$$h = \begin{cases} \varphi, & \text{if } \delta \in [0, \pi] \\ -\varphi, & \text{otherwise,} \end{cases} \quad (47)$$

where

$$\phi = \sqrt{1 - (k_{v,3} + \lambda_{12} \rho v \sin \alpha (\varphi - \alpha))^2} \quad (48)$$

Substitution of  $h$  in Equation (47) to Equation (46) yields

$$\dot{V}_{21} = -\lambda_{12} v^2 \sin^2 \alpha (\varphi - \alpha)^2 < 0. \quad (49)$$

Equation (49) concludes that  $\dot{V}_{21} < 0$  under the necessary condition Equation (44). The control law in Equation (43) can be obtained from substituting Equation (47) to Equation (37) and Equation (38).

*Proposition 5:* The following control law

$$\delta = \begin{cases} \tan^{-1} \gamma_2, & \text{if } h / \sqrt{1 - h^2} \geq 0, \\ -\tan^{-1} \gamma_2, & \text{otherwise,} \end{cases} \quad (50)$$

where

$$\gamma_2 = \sqrt{\left( \frac{(k_{v,3} + \lambda_{12} \rho v \sin \alpha (\varphi - \alpha))^2}{1 - (k_{v,3} + \lambda_{12} \rho v \sin \alpha (\varphi - \alpha))^2} \right)^{-1}} \quad (51)$$

drives  $\dot{V}_{21} < 0$  and  $\dot{V}_{22} < 0$ .

*Proof:* Let  $h$  in Equation (38) is defined as

$$h = -\lambda_2^2 \alpha v. \quad (52)$$

Substitution of  $h$  in Equation (52) to Equation (42) yields

$$\dot{V}_{22} = -\alpha^2 v^2 \lambda_2^2 + \phi \omega^r. \quad (53)$$

In addition, to make Equation (51) decreases  $V_{21}$ ,  $\lambda_2$  must be set such that the following equation is satisfied:

$$\sqrt{1 - (k_{v,3} + \lambda_{12} \rho v \sin \alpha (\varphi - \alpha))^2} = -\lambda_2^2 \alpha v. \quad (54)$$

From Equation (54), we obtain the formulation of  $\lambda_2$  as follows:

$$\lambda_2 = \sqrt[4]{\left(1 - \left(k_{v,3} + \lambda_{1^2} \rho v \sin \alpha (\varphi - \alpha)\right)^2\right) / l^2 \alpha^2 v^2}. \quad (55)$$

It is straightforward that substitution of  $\lambda_2$  in (55) to Equation (52) followed by substitution of Equation (52) to Equation (37) yields Equation (51). ■

*Proposition 6:* The necessary condition to guarantee  $\dot{V}_2 < 0$  is

$$k_{v,3} = k_{v,4} (1 - 2\lambda_{1^2} \rho v \sin \alpha (\varphi - \alpha)). \quad (56)$$

where  $0 < k_{v,4} \leq 1$  is a constant.

*Proof:* From the control law in Equation (43), it is clear that  $k_{v,3} \leq 1 - \lambda_{1^2} \rho v \sin \alpha (\varphi - \alpha)$  to make the argument of  $\tan^{-1}$  real. Also, from the control law in Equation (51), the range of  $k_{v,3}$  must be  $k_{v,3} \geq -\lambda_{1^2} \rho v \sin \alpha (\varphi - \alpha)$  to guarantee  $\dot{V}_2 < 0$ . In summary, we can conclude that the range of  $k_{v,3}$  is

$$-\lambda_{1^2} \rho v \sin \alpha (\varphi - \alpha) \leq k_{v,3} \leq 1 - \lambda_{1^2} \rho v \sin \alpha (\varphi - \alpha) \quad (57)$$

By letting  $k_{v,3} = k_{v,4} (1 - 2\lambda_{1^2} \rho v \sin \alpha (\varphi - \alpha))$ , we can guarantee that  $k_{v,3}$  satisfies Equation (42). Therefore, this proposition is proved. ■

According to Equation (56), the range of  $k_{v,3}$  can be enlarged by increasing the value of  $\lambda_1$ .

#### 4. SIMULATION RESULTS

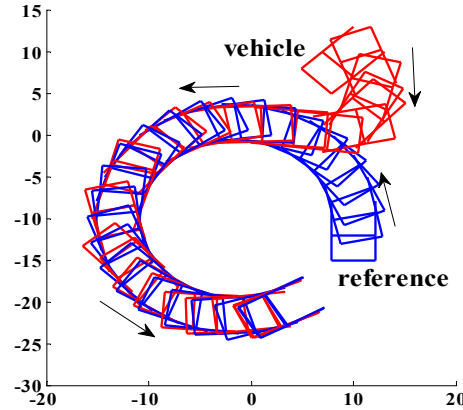


FIGURE 4. The resulted trajectory for  $k_{v,4} = 0.1$ .

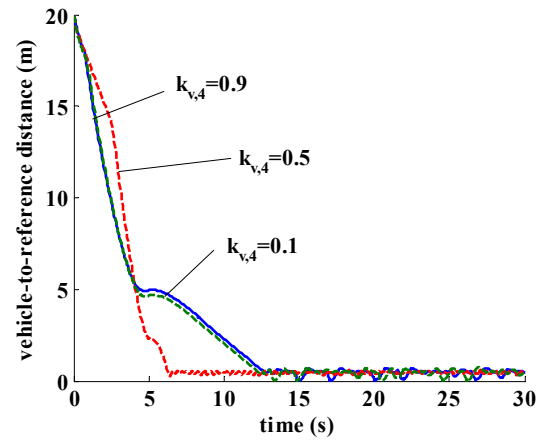


FIGURE 5. The resulted AGV-to-reference distance in various  $k_{v,4}$ .

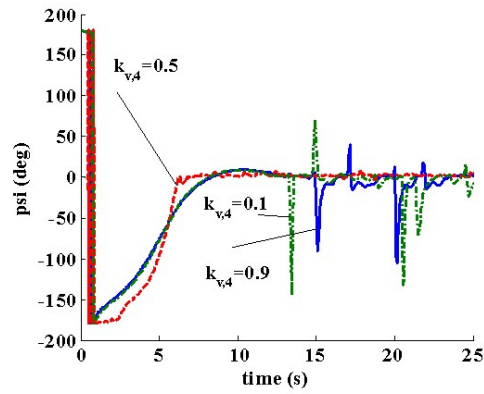


FIGURE 6. The resulted progress of  $\alpha$  under various  $k_{v,4}$ .

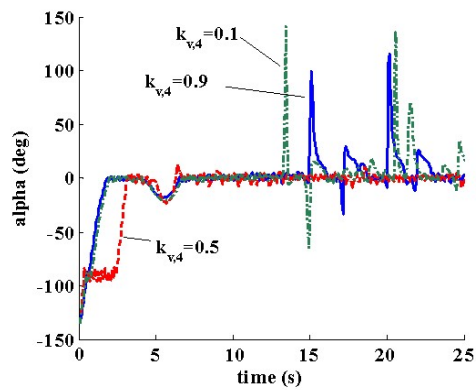


FIGURE 7. The resulted progress of  $\varphi$  in various  $k_{v,4}$

For the AGV,  $x = 10\text{m}$ ,  $y = 10\text{ m}$ ,  $\theta = 45^\circ$ . The reference starts from  $x_r = 10\text{ m}$ ,  $y_r = -10\text{ m}$ ,  $\theta = 90^\circ$ . Therefore, the initial navigation variables are  $\rho = 20\text{ m}$ ,  $\alpha = -135^\circ$ , and  $\varphi = 180^\circ$ . The initial values of the AGV's actuators are  $v = 0\text{ m/s}$  and  $\delta = 0^\circ$ . The reference's velocities are  $v_r = 2\text{ m/s}$  and  $\omega_r = 10^\circ/\text{s}$ .

Here, the following parameters are applied:  $\lambda_1 = 100$ ,  $k_{v,4} = 0.1$ ,  $k_{v,4} = 0.5$  and  $k_{v,4} = 0.9$ . The generated path for  $k_{v,4} = 0.1$  is shown in Figure4. All simulations show similar pattern in distance reduction. There are three phases of distance reduction under extreme initial orientations, as shown in Figure5.

The first phase is the motion of turning the orientation such that  $\alpha$  goes to the interval  $[-\pi/2\text{ rad}, \pi/2\text{ rad}]$ . In the simulations with  $k_{v,4} = 0.1$ ,  $k_{v,4} = 0.5$ , and  $k_{v,4} = 0.9$ , this phase occurs in time interval  $t = [0\text{ s}, 4.5\text{ s}]$ ,  $t = [0\text{ s}, 4.8\text{ s}]$ , and  $t = [0\text{ s}, 4.5\text{ s}]$ , respectively.

The second phase is adjusting  $\varphi$  goes to the interval  $[-\pi/2\text{ rad}, \pi/2\text{ rad}]$ . In the simulation with  $k_{v,4} = 0.1$ ,  $k_{v,4} = 0.5$ , and  $k_{v,4} = 0.9$  this phase occurs in time interval  $t = [4.5\text{ s}, 13\text{ s}]$ ,  $t = [4.8\text{ s}, 6.0\text{ s}]$ , and  $t = [4.5\text{ s}, 12.8\text{ s}]$ , respectively. The visualizations of the results are depicted in Figs. 6 and 7. According to the three simulations, the distance reduction is slower than the first phase. This phenomenon has a strong relationship to the trend of trajectory of  $\varphi$  that moves to zero.

The tracking process then goes to the last phase, i.e., zeroing the AGV-to-reference distance. As mentioned in [15], making  $\rho$  staying zero as time goes to infinity is complicated. The maximum steady-state distance  $\rho_{ss}$  is approximately 0.3-0.5 m.

## 5. CONCLUSIONS

A trajectory tracking control algorithm with AGV-reference distance paradigm for rear-steered AGV is proposed. The main purpose of the controller is to reduce AGV-to-reference distance under the extreme initial navigation variables. Simulations show that the process of tracking consists of three phases: adjusting  $\alpha$  to zero followed by adjusting  $\varphi$  to zero, and finally make the AGV closer to its reference by driving  $\rho$  closer to zero. This research is planned to continue to some aspects of this type of control, such as determining the maximum allowable time to drive the AGV to the maximum steady-state distance.

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